Minimum Wage Analysis with MICE

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Objective

The aim of this vignette is to replicate and enhance Card and Krueger's (1994) analysis of the effect of an increase in the minimum wage on unemployment by using Multivariate Imputation by Chained Equations (MICE). Therefore, this vignette will show how to multiply impute Card and Krueger's dataset and how to obtain the imputed data for the econometric analysis. The main objective is to increase your knowledge and understanding on applications of multiple imputation.

The scientific estimand

In this exercise, we are interested in analyzing the effect that an increase in the minimum wage had on employment.

Background: One of the most famous uses of Difference-in-difference is by Card and Krueger (1994) on the effect of increasing the minimum wage on unemployment. We are going to replicate some of their results.

Experiment: On April 1, 1992, the minimum wage in New Jersey was raised from \$4.25 to \$5.05. In the neighbouring state of Pennsylvania, however, the minimum wage remained constant at \$4.25. Card and Krueger (1994) analyzed the impact of the minimum wage increase on employment in the fast-food industry, a sector which employs many low-wage workers.

The authors collected data on the number of employees in 331 fast-food restaurants in New Jersey and 79 in Pennsylvania. The survey was conducted in February 1992 (before the minimum wage was raised) and in November 1992 (after the minimum wage was raised).

Data: The file $m_wage.csv$ (in the folder) includes the information necessary to replicate Card and Krueger's analysis. The dataset is stored in a "wide" format, i.e. there is a single row for each unit (restaurant), and different columns for the outcomes and covariates in different years. The dataset includes the following variables (as well as others which we will not use):

| Variable name | Description |
|---------------|---|
| nj | dummy equal to 1 if the restaurant is located in NJ |
| emptot | total number of full-time employed pre-treatment |
| emptot2 | total number of full-time employed post-treatment |
| $wage_st$ | average starting wage in the restaurant, pre-treatment |
| $wage_st2$ | average starting wage in the restaurant, post-treatment |
| pmeal | average price of a meal in the pre-treatment period |
| pmeal 2 | average price of a meal in the post-treatment period |
| co_owned | dummy variable equal to 1 if restaurant was co-owned |
| bk | dummy variable equal to 1 if restaurant was a Burger King |
| kfc | dummy variable equal to 1 if restaurant was a KFC |
| wendys | dummy variable equal to 1 if restaurant was Wendys |

We first load and transform the data to a *long* format with the following commands.

```
## Loading wide data
min_wage <- read.csv("m_wage.csv", header=TRUE, stringsAsFactors=FALSE)</pre>
                              min wage[,c("nj","wage st","emptot","kfc",
min wage feb
                    <-
"wendys", "co_owned")]
min_wage_nov
                            min_wage[,c("nj","wage_st2","emptot2","kfc",
                <-
"wendys", "co owned")]
## Create a treatment period indicator
min_wage_feb$treatment <- 0</pre>
min wage nov$treatment <- 1</pre>
## Make sure the two data.frames have the same column names
colnames(min_wage_nov) <- colnames(min_wage_feb)</pre>
## Stack the data.frames on top of one another
mwl <- rbind(min_wage_feb, min_wage_nov)</pre>
rm(min_wage,min_wage_feb,min_wage_nov)
```

The mwl dataset contains 820 observations on 7 variables: *nj*, *wage_st*, *emptot*, *kfc*, *wendys*, *co_owned*, and *treatment*.

Working with mice

1. Load the packages mice and lattice

```
require(mice)
require(lattice)
set.seed(123)
```

If mice is not yet installed, run:

install.packages("mice")

2. Get an overview of the data by the summary() command:

summary(mwl)

| nj | wage_st | emptot | kfc |
|----------------|----------------|---------------|----------------|
| Min. :0.0000 | Min. :4.250 | Min. : 0.00 | Min. :0.0000 |
| 1st Qu.:1.0000 | 1st Qu.:4.500 | 1st Qu.:14.50 | 1st Qu.:0.0000 |
| Median :1.0000 | Median :5.000 | Median :20.00 | Median :0.0000 |
| Mean :0.8073 | Mean :4.806 | Mean :21.03 | Mean :0.1951 |
| 3rd Qu.:1.0000 | 3rd Qu.:5.050 | 3rd Qu.:25.50 | 3rd Qu.:0.0000 |
| Max. :1.0000 | Max. :6.250 | Max. :85.00 | Max. :1.0000 |
| | NA's :41 | NA's :26 | |
| wendys | co_owned | treatment | |
| Min. :0.0000 | Min. :0.0000 | Min. :0.0 | |
| 1st Qu.:0.0000 | 1st Qu.:0.0000 | 1st Qu.:0.0 | |
| Median :0.0000 | Median :0.0000 | Median :0.5 | |
| Mean :0.1463 | Mean :0.3439 | Mean :0.5 | |
| 3rd Qu.:0.0000 | 3rd Qu.:1.0000 | 3rd Qu.:1.0 | |
| Max. :1.0000 | Max. :1.0000 | Max. :1.0 | |

3. Inspect the missing data pattern

Check the missingness pattern for the mwl dataset and comment. Use both md.pattern and md.pairs.

md.pattern(mwl)



Single imputation methods

4. Estimate the effect of the increase of minimum wage on employment

To estimate the effect of the increase in minimum wage on employment we are interested in fitting the model

 $emptot_{it} = \beta_0 + \beta_1 n j_i + \beta_2 treatment_t + \beta_3 n j_i \times treatment_t + \epsilon_{it}.$

The effect is then captured by the β_3 parameter.

Fit the model with the original dataset. You only need to type *nj*treatment* in R so that it includes the three regressors (*nj,treatment,njXtreatment*), they are called the interaction terms.

```
fit <- with(mwl, lm(emptot ~ nj*treatment))
summary(fit)</pre>
```

```
Call:
lm(formula = emptot ~ nj * treatment)
Residuals:
            1Q Median 3Q
    Min
                                     Max
-21.166 -6.439 -1.027 4.473 64.561
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)23.3311.07221.767<2e-16 ***</th>nj-2.8921.194-2.4230.0156 *treatment-2.1661.516-1.4290.1535
nj:treatment 2.754
                          1.688 1.631 0.1033
- - -
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 9.406 on 790 degrees of freedom
 (26 observations deleted due to missingness)
Multiple R-squared: 0.007401, Adjusted R-squared: 0.003632
F-statistic: 1.964 on 3 and 790 DF, p-value: 0.118
```

5. Impute the missing data in the mwl dataset with mean imputation and re-estimate the model

imp <- mice(mwl, method = "mean", m = 1, maxit = 1)</pre>

iter imp variable
1 1 wage_st emptot

```
fit <- with(imp, lm(emptot ~ nj*treatment))
summary(fit)</pre>
```

| # | A tibble: 4 | × 6 | | | | |
|---|--------------|-------------|----------------------|-------------|-------------|-------------|
| | term | estimate | <pre>std.error</pre> | statistic | p.value | nobs |
| | <chr></chr> | <dbl></dbl> | <dbl></dbl> | <dbl></dbl> | <dbl></dbl> | <int></int> |
| 1 | (Intercept) | 23.3 | 1.04 | 22.3 | 1.09e-86 | 820 |
| 2 | nj | -2.82 | 1.16 | -2.43 | 1.53e- 2 | 820 |
| 3 | treatment | -2.11 | 1.47 | -1.43 | 1.52e- 1 | 820 |
| 4 | nj:treatment | 2.68 | 1.64 | 1.64 | 1.02e- 1 | 820 |

6. Impute the missing data with stochastic regression imputation and re-estimate the model.

```
imp <- mice(mwl, method = "norm.nob", m = 1, maxit = 1)

iter imp variable
1 1 wage_st emptot

fit <- with(imp, lm(emptot ~ nj*treatment))
summary(fit)

# A tibble: 4 × 6
  term    estimate std.error statistic p.value nobs
  <chr>        <dbl>        <dbl>
```

Multiple imputation

7. Impute the missing data in the mwl dataset using default mice options.

imp <- mice(mwl,print = FALSE)</pre>

8. Extract the completed data

By default, mice() calculates five (m = 5) imputed data sets. Use the complete() function to get the second imputed data set and examine it using md.pattern().



| | nj | wage_st | emptot | kfc | wendys | co_owned | treatment | |
|-----|----|---------|--------|-----|--------|----------|-----------|---|
| 820 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 |
| | 0 | 0 | 0 | 0 | Θ | 0 | 0 | 0 |

9. Vary the number of imputations.

The number of imputed data sets can be specified by the $m = \ldots$ argument. Create ten imputed data sets. Use seed= for reproducibility.

imp <- mice(mwl, m = 10, print = FALSE, seed = 123)</pre>

10. Inspect the convergence of the algorithm

The mice() function implements an iterative Markov Chain Monte Carlo type of algorithm. Look at the trace lines generated by the algorithm to study convergence and comment.

plot(imp)



Iteration

11. Change the imputation method

For each column, the algorithm requires a specification of the imputation method. To see which method was used by default:

imp\$meth

nj wage_st emptot kfc wendys co_owned treatment

Change the imputation method for emptot to Bayesian normal linear regression imputation.

```
ini <- mice(mwl, maxit = 0)
meth <- ini$meth
meth</pre>
```

| nj | wage_st | emptot | kfc | wendys | co_owned | treatment |
|----|---------|--------|-----|--------|----------|-----------|
| | "pmm" | "pmm" | | | | |

```
meth["emptot"] <- "norm"
meth</pre>
```

| nj | wage_st | emptot | kfc | wendys | co_owned | treatment |
|----|---------|--------|-----|--------|----------|-----------|
| | "pmm" | "norm" | | | | |

and run the imputations again using the same number of imputations and seed as before.

imp <- mice(mwl, meth = meth, m=10, print = FALSE)</pre>

Plot the trace lines to study convergence.

plot(imp)



Iteration

12. Further diagnostic checking.

Use function stripplot() and comment on the results. Are all imputations valid?

stripplot(imp, emptot ~ .imp, pch = 20, cex = 2)



14. Change the imputation method again

Change the imputation method for emptot to CART imputation.

```
ini <- mice(mwl, maxit = 0)
meth <- ini$meth
meth["emptot"] <- "cart"
imp <- mice(mwl, meth = meth, m=10, print = FALSE)</pre>
```

Examine the diagnostic plots and comment.

plot(imp)



Iteration

Obtain the stripplot and comment.

stripplot(imp, emptot ~ .imp, pch = 20, cex = 2)



Repeated analysis in mice

15. Perform the regression for the minimum wage effect analysis on the multiply imputed data. Store the solution in object fit and comment on the estimates.

```
fit <- with(imp, lm(emptot ~ nj*treatment))</pre>
fit
call :
with.mids(data = imp, expr = lm(emptot ~ nj * treatment))
call1 :
mice(data = mwl, m = 10, method = meth, printFlag = FALSE)
nmis :
                    emptot kfc wendys co owned treatment
      nj
         wage_st
                     26
                                0
       0
              41
                                           0
                                                    0
                                                             0
analyses :
[[1]]
Call:
lm(formula = emptot ~ nj * treatment)
Coefficients:
(Intercept)
                          treatment nj:treatment
                    nj
                -3.235
     23.633
                              -2.478
                                           3.177
[[2]]
Call:
lm(formula = emptot ~ nj * treatment)
Coefficients:
                nj
(Intercept)
                            treatment nj:treatment
                -2.903
     23.348
                             -2.168
                                            2.811
[[3]]
Call:
lm(formula = emptot ~ nj * treatment)
Coefficients:
 (Intercept)
                            treatment nj:treatment
                    nj
     23,589
                -3.099
                              -2.446
                                            3.074
```

```
[[4]]
Call:
lm(formula = emptot ~ nj * treatment)
Coefficients:
      ercept) nj treatment nj:treatment
23.278 -2.776 -1.940 2.559
 (Intercept)
[[5]]
Call:
lm(formula = emptot ~ nj * treatment)
Coefficients:
 (Intercept)
                    nj treatment nj:treatment
    23.633 -3.190
                              -2.661 3.395
[[6]]
Call:
lm(formula = emptot ~ nj * treatment)
Coefficients:
      ercept) nj treatment nj:treatment
23.810 -3.358 -2.345 3.070
 (Intercept)
[[7]]
Call:
lm(formula = emptot ~ nj * treatment)
Coefficients:<br/>(Intercept)njtreatmentnj:treatment23.528-3.093-2.3863.172
[[8]]
Call:
lm(formula = emptot ~ nj * treatment)
Coefficients:
 (Intercept)
                        nj
                               treatment nj:treatment
```

```
23.380
                  -3.062
                               -2.009
                                             2.818
[[9]]
Call:
lm(formula = emptot ~ nj * treatment)
Coefficients:
 (Intercept)
                            treatment nj:treatment
                  nj
     23.272 -2.858
                               -1.991
                                             2.667
[[10]]
Call:
lm(formula = emptot ~ nj * treatment)
Coefficients:
 (Intercept)
                            treatment nj:treatment
                     nj
     23.633
                  -3.228
                               -2.234
                                             2,933
```

16. Pool the analyses from object fit and comment.

```
pool.fit <- pool(fit)
summary(pool.fit)</pre>
```

```
termestimatestd.errorstatisticdfp.value1(Intercept)23.5104431.07431521.884118726.33536.246713e-822nj-3.0803071.192782-2.582456745.97529.999436e-033treatment-2.2658231.516192-1.494417743.15431.354911e-014nj:treatment2.9676351.6860121.760151749.81167.878986e-02
```

17. Squeezing the imputations by Bayesian normal linear regression imputation

Use mice post-processing to constraint the imputations for *emptot* to being positive.

```
ini <- mice(mwl, maxit = 0)
meth <- ini$meth
meth["emptot"] <- "norm"
imp <- mice(mwl, meth = meth, m=10, print = FALSE)</pre>
```

Squeeze the imputed values to be between 0 and 90.

```
post <- ini$post
post["emptot"] <- "imp[[j]][, i] <- squeeze(imp[[j]][, i], c(0, 90))"
imp <- mice(mwl, meth=meth, post=post, print=FALSE)</pre>
```

Obtain the stripplot and comment.

stripplot(imp, emptot ~ .imp, pch = 20, cex = 2)



18. Perform the regression for the minimum wage effect analysis on the multiply imputed data just squeezed. Store the solution in object fit and comment on the estimates.

```
fit <- with(imp, lm(emptot ~ nj*treatment))
fit</pre>
```

```
call :
with.mids(data = imp, expr = lm(emptot ~ nj * treatment))
call1 :
mice(data = mwl, method = meth, post = post, printFlag = FALSE)
nmis :
                                     kfc
       nj
            wage st
                       emptot
                                            wendys
                                                    co owned treatment
        0
                 41
                           26
                                       0
                                                 0
                                                            0
                                                                      0
```

```
analyses :
[[1]]
Call:
lm(formula = emptot ~ nj * treatment)
Coefficients:
     tercept)njtreatmentnj:treatment23.352-2.886-2.2282.736
 (Intercept)
[[2]]
Call:
lm(formula = emptot ~ nj * treatment)
Coefficients:
 (Intercept) nj treatment nj:treatment
23.620 -3.002 -2.433 3.044
[[3]]
Call:
lm(formula = emptot ~ nj * treatment)
Coefficients:
      ercept) nj treatment nj:treatment
23.387 -2.993 -1.915 2.474
 (Intercept)
[[4]]
Call:
lm(formula = emptot ~ nj * treatment)
Coefficients:<br/>(Intercept)njtreatmentnj:treatment23.339-2.715-2.0062.327
[[5]]
Call:
lm(formula = emptot ~ nj * treatment)
Coefficients:
```

| (Intercept) | nj | treatment | nj:treatment |
|-------------|--------|-----------|--------------|
| 23.439 | -2.972 | -2.326 | 3.089 |

19. Pool the analyses from object fit and comment.

```
pool.fit <- pool(fit)
summary(pool.fit)</pre>
```

```
termestimatestd.errorstatisticdfp.value1(Intercept)23.4275731.06821621.931488773.37812.801035e-832nj-2.9135161.187961-2.452534780.51141.440327e-023treatment-2.1816811.518957-1.436302709.66161.513570e-014nj:treatment2.7338241.7101171.598618545.32181.104847e-01
```

20. Binary missing data.

Generate 25 missing data in the *co_owned* variable using the sample() function and random seed as before. Call the new dataset *nmwl* making sure to define the *co_owned* variable as categorical using the as.factor().

```
set.seed(123)
miss_ind = sample(820,25)
nmwl= mwl
nmwl$co_owned[miss_ind] = NA
nmwl$co_owned = as.factor(nmwl$co_owned)
```

21. Examine the pattern of missing data

Obtain the missing data pattern and comment.

md.pattern(nmwl)



| | nj | kfc | wendys | treatment | co_owned | emptot | wage_st | | |
|-----|----|-----|--------|-----------|----------|--------|---------|----|--|
| 738 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | |
| 33 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | |
| 17 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 1 | |
| 7 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 2 | |
| 22 | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 1 | |
| 1 | 1 | 1 | 1 | 1 | 0 | 1 | 0 | 2 | |
| 2 | 1 | 1 | 1 | 1 | 0 | 0 | 1 | 2 | |
| | 0 | 0 | 0 | Θ | 25 | 26 | 41 | 92 | |

md.pairs(nmwl)

| \$rr | | | | | | | |
|-----------|------|-----------|----------|---|----------|------------|-----------|
| | nj | wage_st | emptot | kfc | wendys | co_owned | treatment |
| nj | 820 | 779 | 794 | 820 | 820 | 795 | 820 |
| wage_st | 779 | 779 | 760 | 779 | 779 | 755 | 779 |
| emptot | 794 | 760 | 794 | 794 | 794 | 771 | 794 |
| kfc | 820 | 779 | 794 | 820 | 820 | 795 | 820 |
| wendys | 820 | 779 | 794 | 820 | 820 | 795 | 820 |
| co_owned | 795 | 755 | 771 | 795 | 795 | 795 | 795 |
| treatment | 820 | 779 | 794 | 820 | 820 | 795 | 820 |
| | | | | | | | |
| \$rm | | | | | | | |
| | nj v | vage_st e | emptot A | <fc td="" v<=""><td>vendys o</td><td>co_owned t</td><td>treatment</td></fc> | vendys o | co_owned t | treatment |
| nj | 0 | 41 | 26 | 0 | Θ | 25 | 0 |
| | | | | | | | |

| wage_st | 0 | Θ | 19 | 0 | Θ | 24 | Θ |
|-----------|----|---------|--------|-----|--------|----------|-----------|
| emptot | 0 | 34 | Θ | 0 | Θ | 23 | Θ |
| kfc | 0 | 41 | 26 | 0 | 0 | 25 | Θ |
| wendys | 0 | 41 | 26 | 0 | 0 | 25 | Θ |
| co_owned | 0 | 40 | 24 | 0 | 0 | Θ | Θ |
| treatment | 0 | 41 | 26 | 0 | 0 | 25 | Θ |
| | | | | | | | |
| \$mr | | | | | _ | | |
| _ | nj | wage_st | emptot | kfc | wendys | co_owned | treatment |
| nj | 0 | 0 | 0 | 0 | 0 | 0 | Θ |
| wage_st | 41 | 0 | 34 | 41 | 41 | 40 | 41 |
| emptot | 26 | 19 | 0 | 26 | 26 | 24 | 26 |
| kfc | 0 | 0 | 0 | 0 | 0 | 0 | Θ |
| wendys | 0 | 0 | 0 | 0 | 0 | 0 | Θ |
| co_owned | 25 | 24 | 23 | 25 | 25 | 0 | 25 |
| treatment | 0 | 0 | 0 | 0 | 0 | Θ | Θ |
| | | | | | | | |
| \$mm | | | | | | | |
| | nj | wage_st | emptot | kfc | wendys | co_owned | treatment |
| nj | 0 | 0 | 0 | 0 | 0 | 0 | Θ |
| wage_st | 0 | 41 | 7 | 0 | 0 | 1 | Θ |
| emptot | 0 | 7 | 26 | 0 | 0 | 2 | Θ |
| kfc | 0 | 0 | Θ | 0 | 0 | Θ | Θ |
| wendys | 0 | 0 | 0 | 0 | Θ | 0 | Θ |
| co_owned | 0 | 1 | 2 | 0 | Θ | 25 | Θ |
| treatment | 0 | 0 | 0 | 0 | 0 | 0 | Θ |

21. Impute the missing data and examine the method selected for the binary variable

```
ini <- mice(nmwl, maxit = 0)
meth <- ini$meth
meth</pre>
```

| nj | wage_st | emptot | kfc | wendys | co_owned | treatment |
|----|---------|--------|-----|--------|----------|-----------|
| | "pmm" | "pmm" | | | "logreg" | |

22. Change the imputation method one last time

Change the imputation method for emptot to linear regression with bootstrap and logistic regression with bootstrap for co_owned.

```
ini <- mice(nmwl, maxit = 0)
meth <- ini$meth
meth["emptot"] <- "norm.boot"
meth["co_owned"] <- "logreg.boot"
imp <- mice(nmwl, meth = meth, m=10, print = FALSE)</pre>
```

Diagnostic checks.

plot(imp)



stripplot(imp, emptot + co_owned ~ .imp, pch = 20, cex = 2)



Compare the predictions to the true values for *co_owned*.

cbind(mwl\$co_owned[miss_ind],imp\$imp\$co_owned[])

| | <pre>mwl\$co_owned[miss_ind]</pre> | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|-----|------------------------------------|---|---|---|---|---|---|---|---|---|----|
| 14 | 1 | 0 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 1 | 1 |
| 26 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 0 |
| 91 | Θ | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 1 | 0 | 0 |
| 118 | Θ | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 179 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 1 |
| 195 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 229 | Θ | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 0 | 0 | 0 |
| 244 | Θ | 1 | 1 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 |
| 299 | 1 | 0 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| 348 | Θ | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 0 |
| 355 | Θ | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 1 | 0 |
| 374 | Θ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 415 | Θ | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 0 |
| 426 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 1 |
| 463 | 1 | 0 | 1 | 0 | 0 | 1 | 1 | 0 | 1 | 1 | 0 |
| 519 | Θ | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 526 | Θ | 1 | 0 | 0 | 1 | 1 | 1 | 0 | 1 | 0 | 1 |
| 602 | Θ | 0 | 1 | 1 | 1 | 1 | 0 | 1 | 0 | 0 | 1 |
| 603 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 0 |
| 649 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 0 |
| 665 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| 709 | Θ | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 766 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 1 |
| 768 | Θ | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| 802 | 1 | 1 | 0 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 |

Squeeze the imputed values for *emptot* to be between 0 and 90.

```
post <- ini$post
post["emptot"] <- "imp[[j]][, i] <- squeeze(imp[[j]][, i], c(0, 90))"
imp <- mice(nmwl, meth=meth, post=post, print=FALSE)</pre>
```

23. Perform the regression for the minimum wage effect analysis one last time

Consider the linear regression in the last imputed dataset in the the extended specification controlling for whether the restaurant was co-owned, a Burger King, a KFC, or a Wendys. The specification is

Do your estimates of the treatment effect differ? Are they statistically significant?

```
fit <- with(imp, lm(emptot ~ nj*treatment+co_owned+kfc+wendys))
fit</pre>
```

```
call :
with.mids(data = imp, expr = lm(emptot ~ nj * treatment + co owned +
   kfc + wendys))
call1 :
mice(data = nmwl, method = meth, post = post, printFlag = FALSE)
nmis :
        wage st
                   emptot kfc wendys co owned treatment
      nj
      0
             41
                    26
                              0
                                      0
                                                25
                                                          0
analyses :
[[1]]
Call:
lm(formula = emptot ~ nj * treatment + co_owned + kfc + wendys)
Coefficients:
                 nj
(Intercept)
                         treatment co_owned1
                                                       kfc
    25.5221
                           -2.0957
                                                  -9.8914
              -2.3767
                                      -1.7305
     wendys nj:treatment
    -0.2719 2.7588
[[2]]
Call:
lm(formula = emptot ~ nj * treatment + co_owned + kfc + wendys)
Coefficients:
                 nj
(Intercept)
                         treatment co_owned1
                                                       kfc
                                      -2.0702 -9.8701
    25.7746
              -2.3291
                           -2.3911
    wendys nj:treatment
    -0.3066 2.9189
[[3]]
Call:
lm(formula = emptot ~ nj * treatment + co_owned + kfc + wendys)
Coefficients:
 (Intercept)
                          treatment co_owned1
                                                       kfc
                   nj
               -2.437
                             -2.423
                                         -1.737
     25.675
                                                    -9.867
     wendys nj:treatment
     -0.584
                  2.976
```

[[4]]

```
Call:
lm(formula = emptot ~ nj * treatment + co_owned + kfc + wendys)
Coefficients:
 (Intercept)
                           treatment co owned1
                                                             kfc
                     nj
                 -2.504
     25.572
                              -2.145
                                            -1.830
                                                         -9.789
     wendys nj:treatment
     -0.526
                  2.823
[[5]]
Call:
lm(formula = emptot ~ nj * treatment + co_owned + kfc + wendys)
Coefficients:
 (Intercept)
                     nj
                             treatment co owned1
                                                             kfc
     25.898
                 -2.650
                               -2.612
                                             -2.052
                                                          -9.780
     wendys nj:treatment
     -1.019
                  3.247
pool.fit <- pool(fit)</pre>
summary(pool.fit)
         term
                estimate std.error statistic
                                                   df
                                                          p.value
1 (Intercept) 25.6881482 1.0227476 25.1168024 692.9852 1.732774e-99
2
           nj -2.4591805 1.0762578 -2.2849363 758.3143 2.259189e-02
3
  treatment -2.3332544 1.3744657 -1.6975720 677.6548 9.004771e-02
    co owned1 -1.8840372 0.6591614 -2.8582333 356.8792 4.510091e-03
4
5
          kfc -9.8394792 0.7717286 -12.7499213 802.1252 4.910345e-34
       wendys -0.5414838 0.9248559 -0.5854791 186.9380 5.589317e-01
6
7 nj:treatment 2.9446525 1.5216956 1.9351128 745.3697 5.335444e-02
```

References

Card, David and Krueger, Alan B. (1994). *Minimum Wages and Employment: A Case Study of the Fast-Food Industry in New Jersey and Pennsylvania*. **American Economic Review**, 84(4), pp. 772-93.